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APR 77 W H HARPER, P N MARINOS
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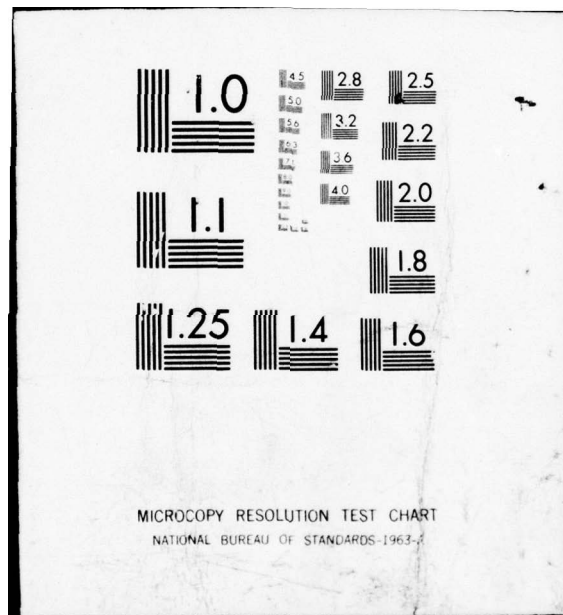
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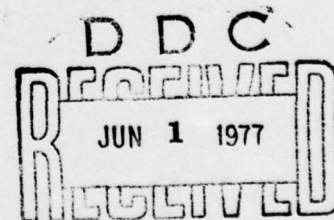
A Method for Computing Vertical-Plane Coverage Diagrams for Frequency Agile Pulse Radar Systems

W. H. HARPER AND PETER N. MARINOS

*Search Radar Branch
Radar Division*

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A METHOD FOR COMPUTING VERTICAL-PLANE COVERAGE DIAGRAMS FOR FREQUENCY AGILE PULSE RADAR SYSTEMS

INTRODUCTION

In a comprehensive report on maximum radar range computations, Blake [1] provides all the necessary tools for obtaining coverage plots (i.e., range-height-angle charts) of monochromatic pulse radar systems. This paper provides a method for extending the range computations applicable to the monochromatic case to pulse radar systems featuring frequency agility. The number of different frequencies employed, as well as the number of consecutive pulses to be transmitted at the same frequency, are both arbitrary.

MATHEMATICAL ANALYSIS

The detection scheme assumed in the analysis which follows utilizes a square-law detector followed by a linear integrator, as shown in Fig. 1. The symbols D_o , X_o , and Y_o denote the SNR (i.e., signal-to-noise power ratio) at the designated points of the detector-integrator complex.

Based on approximate closed-form expressions derived by Barton [2] and later simplified by Cann [3], one may relate the input and output SNRs using the equation

$$X_o = \frac{2D_o^2}{D_o + 2.3} \quad (1)$$

The integrated output SNR, Y_o , may now be written in the form

$$Y_o = \sum_{j=1}^N X_{oj} = \sum_{j=1}^N \left(\frac{2D_{oj}^2}{D_{oj} + 2.3} \right) \quad (2)$$

where N denotes the number of integrated pulses and D_{oj} represents the SNR at the detector input due to the j^{th} pulse illuminating a target located at R_{max} ; it is assumed that R_{max} represents the maximum detection range associated with the total energy delivered on the target by the N transmitted pulses.

Since our objective is to relate the integrated SNR (i.e., Y_o) to a maximum detection range, R_{max} , using the classical radar equation, an average SNR is defined at the detector output in the form

Note: Manuscript submitted March 4, 1977.

$$\hat{X}_O = \frac{1}{N} \sum_{j=1}^N X_{Oj} \approx \frac{1}{N} \sum_{j=1}^N \frac{2D_{Oj}^2}{D_{Oj} + 2.3} \quad (3)$$

The SNR given by Eq. (3) may be thought of as the SNR necessary to achieve a specified probability of detection, P_d , and false alarm, P_{fa} , for a specified number of pulses and a postulated type of target; normally, it is the corresponding SNR, \hat{D}_O , at the input of the square-law detector rather than \hat{X}_O that one associates with P_d and P_{fa} . Given, however, \hat{D}_O , the corresponding value of \hat{X}_O is obtained using Eq. (1). For example, given N , P_d , and P_{fa} , and a target described by Swerling's Case 2, one may utilize published results [1] to determine \hat{D}_O and subsequently X_O .

Once \hat{X}_O is obtained, the problem becomes one of relating \hat{X}_O to a corresponding maximum detection range, R_{max} , in a way which takes advantage of the computational aids developed by Blake [1,4]. This is accomplished by writing the radar equation in the form,

$$D_{Oj} = \frac{P_t A^2 \sigma F_j^4}{4\pi\lambda_j^2 P_{noise} \cdot R_{max}^4} = \left[\frac{P_t A^2 \sigma}{4\pi\lambda_j^2 \hat{D}_O P_{noise}} \right] F_j^4 \cdot \frac{\hat{D}_O}{R_{max}^4} \quad (4)$$

where D_{Oj} represents the SNR at the detector input due to the j^{th} pulse return from a target positioned at R_{max} ; \hat{D}_O is the (averaged) minimum SNR based on N pulses; F_j denotes the pattern-propagation factor; and the remaining symbols in Eq. (4) represent well-known radar parameters [5]. The bracketed portion of Eq. (4) represents the free-space range, R_{jfs}^4 , corresponding to N pulses, but as if they all had been transmitted at frequency f_j (i.e., wavelength λ_j) and each resulted in a SNR, \hat{D}_O , at the detector input. In view of the above interpretation, one may rewrite Eq. (4) in the form,

$$D_{Oj} = \hat{D}_O \left(\frac{R_{xj}}{R_{max}} \right)^4 \quad (5)$$

where $R_{xj} = R_{jfs} F_j$, and $j = 1, 2, \dots, N$.

Since

$$R_{jfs}^4 = \frac{P_t A^2 \sigma}{4\pi\lambda_j^2 \hat{D}_O P_{noise}}, \quad (6)$$

varying only the frequency results in a relationship of the form

$$R_{jfs}^4 = R_{ifs}^4 \left(\frac{\lambda_1}{\lambda_j} \right)^2 = R_{ifs}^4 \left(\frac{f_j}{f_1} \right)^2 \quad (7)$$

which provides the free-space range at frequency f_j in terms of the free-space range at another frequency, f_i , while all other parameters in Eq. (6) remain fixed.

In some instances the maximum free-space range, $R_{j \max}$, based on the number of pulses at each frequency, is known. In this case, there is a \hat{D}_{oj} given by

$$\hat{D}_{oj} = \frac{P_t A^2 \sigma_{Fj}^4}{4\pi\lambda_j^2 P_{\text{noise}} R_{j \max}^4} \quad (8)$$

The free-space range at frequency f_j is then given by

$$R_{jfs}^4 = R_{j \max}^4 \left(\frac{\hat{D}_{oj}}{\hat{D}_o} \right) \quad (9)$$

Substituting next Eqs. (3) and (5) into Eq. (1), that is, into expression

$$\hat{X}_o = \frac{2\hat{D}_o}{1 + 2.3 \left(\frac{1}{\hat{D}_o} \right)} \quad (10)$$

one obtains

$$\frac{1}{1 + \alpha} = \frac{1}{N} \sum_{j=1}^N \left[\frac{\left(\frac{R_{xj}}{R_{\max}} \right)^4}{1 + \alpha \left(\frac{R_{\max}}{R_{xj}} \right)^4} \right] \quad (11)$$

where $\alpha = (2.3/\hat{D}_o)$.

PLOTTING TECHNIQUES

Solution of Eq. (11) for R_{\max} provides the information necessary to produce the so-called radar vertical-plane coverage diagrams.

Blake [4] has developed a computer program for presenting the radar interference lobing phenomena on range-height-angle plots. This program was named LOBEPLOT and was written in Fortran for use on a CDC-3800 computer.

Relatively simple modifications to LOBEPLOT have been made which have resulted in the solution of Eq. (11) and enabled the computer (Calcomp) plotting of the lobing charts for frequency agile radars. The original modifications were made, and the program was debugged on a CDC-3800 computer at NRL. More

recently, the program has been changed to allow running on the new Texas Instruments Advanced Scientific Computer (ASC) at NRL. This new version has been named LOBMUF for "lobes, multi-frequency." The complete program is listed in Appendix A; the input data card formats are given in Appendix B.

In LOBMUF, P_d , P_{fa} , the total number of pulses integrated, the Swerling fluctuation case, and the number of radars or radar frequencies are specified on input data cards. In addition, for each radar or radar frequency, the free-space range, beamwidth, number of pulses at that frequency, sidelobe level, and a parameter FREF are required. FREF is zero if the free-space range was calculated at each frequency as indicated in connection with Eqs. (8) and (9); otherwise, FREF is the midband or average frequency and the free-space range corresponding to this reference frequency. Other inputs to the program are identical to those for LOBEPLLOT. They concern the dimensions of the range-height chart, polarization radiated, antenna height and tilt, etc.

Using subroutines from another of Blake's computer programs [5], RGCALC, the signal-to-noise ratio, \hat{D}_0 , and the parameter, α , are computed. If FREF = 0, \hat{D}_{0j} for each frequency is calculated. Next, the pattern propagation factor, F_j , is calculated exactly as in Blake's LOBEPLLOT. Finally, a simple search routine is used to converge on the value of R_{max} in Eq. (11). The search is terminated when the two sides of Eq. (11) differ by less than 0.01.

Figure 2 gives a typical coverage diagram generated by the computer program LOBMUF. The inputs involved a hypothetical radar radiating two pulses at each of 21 frequencies from 1350 MHz to 1650 MHz in 15 MHz steps. 1500 MHz was chosen as the reference frequency, and the free-space range was chosen to be 100 n. mi.

Figure 3 shows the lobing plot for a single frequency radar at 1500 MHz. A comparison of Figs. 2 and 3 shows that the incoherent integration in a frequency agile radar does much to fill in the nulls of the lobing pattern and give a solid elevation coverage.

SUMMARY

A computer program has been developed to plot range-height-angle lobing charts for frequency agile radars. This program is quite flexible. It may be used to plot the lobing charts for several radars or a single radar including several frequencies. This program, LOBMUF, builds on Blake's range-height charts and lobing plots. The program assumes incoherent integration and a closed form expression for a square-law detector.

ACKNOWLEDGMENT

Thanks are due to Dr. W. M. Waters of NRL for many helpful discussions concerning this problem.

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3. A. J. Cann, "Simple Radar Detection Calculation," IEEE Transactions on Aerospace and Electronic Systems, Vol. AES-8, pp 73-74, Jan 1972
4. L. V. Blake, "Machine Plotting of Radio/Radar Vertical-Plane Coverage Diagrams," NRL Report 7098, Jun 28, 1970
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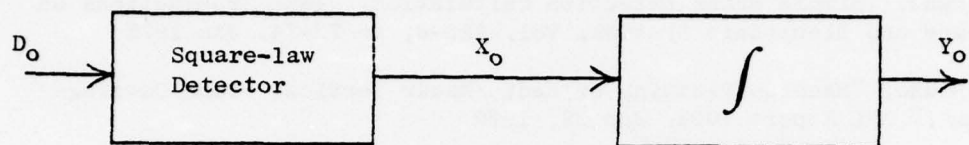
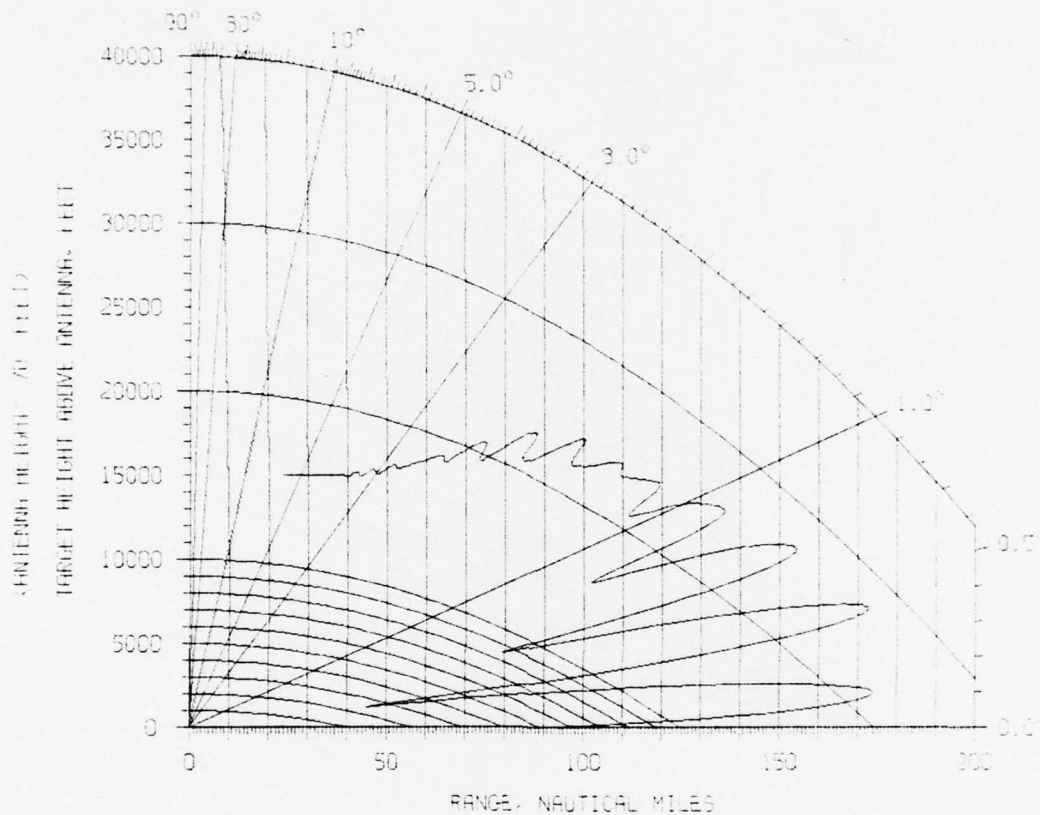


Fig. 1 — Radar detection and integration diagram

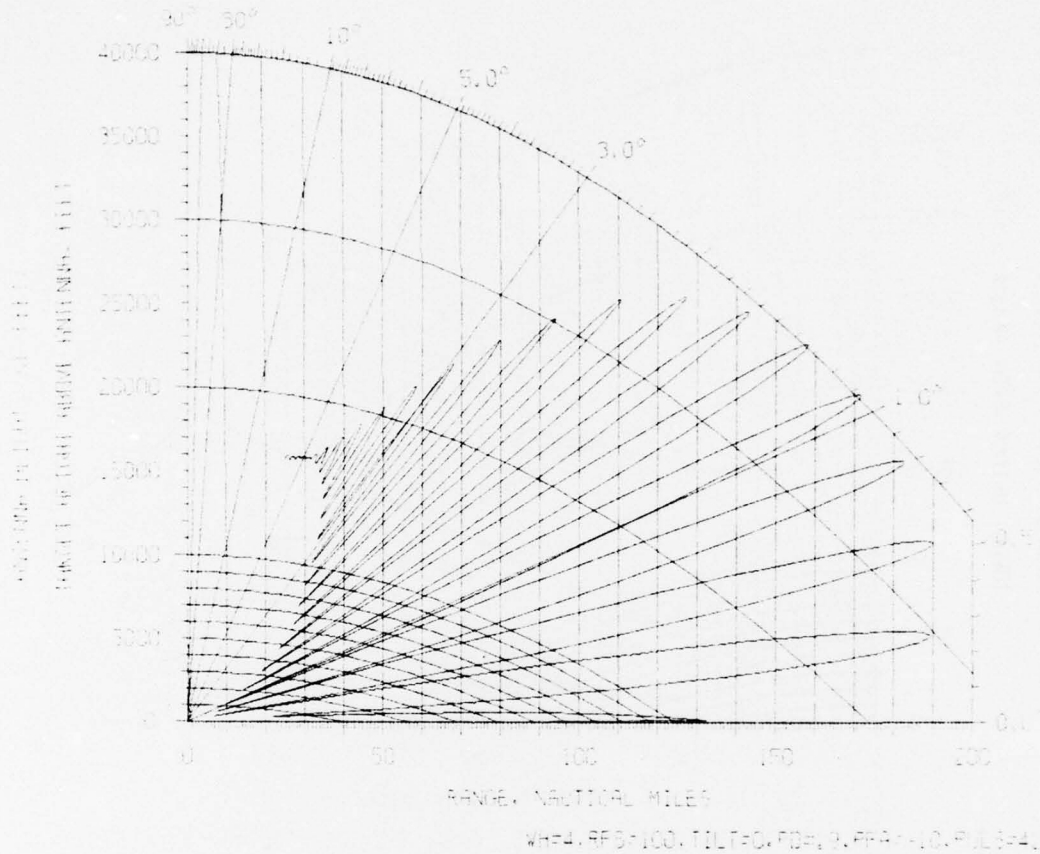
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$F=1.35$ TO 1.65 IN 0.015 STEPS, $WH=4$, $RF=100$, $TILT=0$, $PD=-10$, $PULS=42$

Fig. 2 — Lobing chart for hypothetical radar radiating two pulses at each of 21 frequencies from 1350 MHz to 1650 MHz in 15 MHz steps. Wave height of 4 feet, free-space range of 100 n. mi., and vertical beamwidth of 4.0° were assumed.

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APPENDIX A: Fortran Listing for Program LOBMUF

The basic modifications to Blake's LOBEPLOT for program LOBMUF occur in Subroutine LOBES, as described in the Plotting Techniques section of this report. In addition, Subroutines PDSN, PD, INVERS, MARSWR, DGAM, DEVAL, GAM, EVAL, and SUMLOG are incorporated directly from RGCALC.

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STATEMENT

```
PROGRAM LCBMUF
REAL*8 ILABL(10)
COMMON /MTPE/ Q1,Q2,Q3,Q4,Q5,Q6,ERROR
COMMON/ADPLTS/IAOD
COMMON/CSC/ICSC
COMMON/LT/LTN
DIMENSION A(1500)
DATA LTN/0/
CALL RSTORP
READ 1,ANTHGT
ERROR=0.001
CALL PLOTS (A,1500,0.5)
PRINT 30
30 FORMAT (' TWO PEN TURRET POSITIONS ARE USED, D10 AND D11. PLOT ST
*ARTS WITH PEN TURRET POSITION D10. CHARACTER PEN IS D11. '//)
2 READ (5,5,END=100) ILABL
200 READ 3,XMAX,YMAX,RMAX,HMAX,THMIN,THMAX,WHFT,RDR
NRDR=NRDR
IF ( NRDR .LT. 1 ) GOTO 110
SFAC = YMAX*.125
52 H = .175*SFAC
Y = 1.5*SFAC
IF (LTN .EQ. 18) GO TO 61
IF ((YMAX+Y).LE.9.5) GO TO 61
60 SFAC = 9.5/(YMAX+Y)
YMAX = YMAX*SFAC
XMAX = XMAX*SFAC
Y = Y*SFAC
H = H*SFAC
61 X=Y+3.*H
CALL ORIGIN (X,Y)
PRINT 10, ILABL
CALL RHACHT (XMAX,YMAX,RMAX,HMAX,ANTHGT)
CALL LGBES (XMAX,YMAX,RMAX,HMAX,WHFT,THMIN,THMAX,NRDR)
CALL LETTER(0.,-Y,H,ILABL,0.0,80)
CALL ORIGIN (XMAX+3.*Y,-Y)
CALL REZERP
GO TO 2
100 CALL ENDPLT
GOTO 130
110 PRINT 120,NRDR
120 FORMAT('PROGRAM TERMINATION DUE TO ILLEGAL DATA ENTERED FOR NU
*MBER OF RADAPS . . . . . NUMBER ENTERED IS ',I5)
130 CONTINUE
1 FORMAT (F10.0)
3 FORMAT( BF10.0)
5 FORMAT (10A8)
10 FORMAT(3X,10A8//)
END
```


STATEMENT

```

SUBROUTINE L08ES (XMAX,YMAX,RMAX,HMAX,WHFT,THMIN,THMAX,NRDR)
C   THIS VERSION COMPLETED JUNE 1976 TO ALLOW PLOTTING LOBING PATTERN
C   FOR MULTIFREQUENCY CASE WITH INCOHERENT INTEGRATION.
COMMON/CSC/ICSC
COMMON /MTPE/ X2, Y2, X11, Y11, XA, YA, ERROR
COMMON/9/XX(181),YY(181),CT1(181),SN1(181),DELL
COMMON/DUM1/PFF( 2000 )
DIMENSION RXN4(50),NUM(50),SNP(50)
DIMENSION RFS(50),FMHZ(50),B*D(50),SLDB(50)
DATA IIMAX/2000/
DATA ICSC / 0/
DATA PI/3.141592654/
DATA PI2/6.283185307/
DATA RDN/.01745329252/
DATA CNV/1.645788333E-4/
DATA AE / 2.786526684E7/
NRDS=NRDR
RNO=FLRAT(NRDS)
READ 904,PDT,PFA,PULS,CASE,AHFT,TILT,POL,CSC
PRINT 905,PDT,PFA,PULS,CASE,AHFT,TILT,POL,CSC
905 FORMAT (/ ,2X,4HPDT=,F5.2,2X,4HPFA=,F5.2,2X,5HPULS=,F6.1,2X,5HCASE=
*,F5.2,2X,5HAHFT=,F6.1,2X,5HTILT=,F5.2,2X,4HPOL=,F4.1,2X,4HCSC=,F4.
*,1,/)
NPULS=PULS
KASE=CASE
CALL PDSN (PDT,PFA,NPULS,KASE,SDR)
SNN=10.**(SDR/10.)
GAMMA=2.3/SNN
BETA=1./(1.+GAMMA)
904 FORMAT (8F10.0)
PRINT 590
590 FORMAT(' THE CALLING PARAMETERS SENT TO SUBROUTINE L08ES ARE AS FO
*LL0WS')
PRINT 591 , XMAX , YMAX , RMAX , HMAX , WHFT , THMIN , THMAX , NRDR
591 FORMAT(2X,5HXMAX=,F4.1,2X,5HYMAX=,F4.1,2X,5HRMAX=,F6.1,2X,5HHMAX=,
*,F9.1,2X,5HWHFT=,F5.1,2X,6HTHMIN=,F4.1,2X,6HTHMAX=,F4.1,2X,5HNRDR=
*,13)
DO 84 II=1,IIMAX
84 PFF(II) = 0.0
E = YMAX*RMAX/(XMAX*HMAX*CNV)
EX=XMAX/RMAX
Z=WHFT*.3535534
XP=1,E=45
YP=1,E=45
DO 801 JJ=1,NRDS
801 READ (5,802,END=807) RANGE,FREQ,BEAM,SLDB,PULNUM,FREF
ICSC=CSC
IPOL=POL
NUM(JJ)=PULNUM
RFS(JJ)=RANGE
FMHZ(JJ)=FREQ

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      RAD(JJ)=REAM
      SLDB(JJ)=SCLAB
402  FORMAT (6F10.0)
      PRINT 499 , NRDR
499  FORMAT (//,20X,'THE RADAR PARAMETERS INPUT FOR RADAR NUMBER  ',I3
      *,'  ARE AS FOLLOWS')
      PRINT 592,RFS(JJ),AHFT,FMHZ(JJ),BWD(JJ),SLDB(JJ),TILT,POL,CSC,PULN
      *UN,FREF
592  FORMAT (/,2X,4HREFS=F6.1,2X,5HAHFT=F6.1,2X,5HFMHZ=F7.1,2X,4HBWD=F
      *F5.1,2X,5HSLDB=F5.1,2X,5HTILT=F5.1,2X,4HPOL=F2.0,2X,4HCSC=F2.0
      *,2X,6HPULS=F5.0,2X,5HFREF=F7.1/)
      IF (FREF.NE.0.) GO TO 514
      CALL PDSPN (PDT,PFA,NUM(JJ),KASE,SDR)
      SNR(JJ)=10.** (SDR/10.)
      GO TO 515
514  SNR(JJ)=SNN
      RFS(JJ)=RFS(JJ)*SQRT(SQRT(FMHZ(JJ)/FREF))
515  CONTINUE
      RFS(JJ)=RFS(JJ)*(SQRT(SQRT(SNR(JJ)/SNN)))
      NRDR=NRDR+1
801  CONTINUE
      TILTR = TILT + RDN
      THMINR=THMIN+RDN
      THMAXR=THMAX+RDN
      DEL1 = ( THMAXR - THMINR ) / IIMAX
      PI23DE = 3.0*DEL1 + PI2
      THET2=THMINR+DEL1
      N = 0
      INDEX = 0
      F=1.5
      IDASH=1
      CALL DASHFN
      AH2=AHFT*AHFT
      HAE = 2. * AHFT/(3.*AE)
      AEH = AE * (AE + AHFT)
      PARAM = SQRT (AE/(2.*AHFT))
      DO 810  II= 1,IIMAX
      PF4=0.
      THET2 = THET2 + DEL1
      IF (THET2 .GE. PI23DE      ) GOTO 40
      T2 = TAN (THET2)
      S2 = SIN(THET2)
      S3 = S2
      PSI = THET2
      DO 805  M=1,NRDS
      BWR=BWD(M)*RDN
      BW2 = BWR*.5
      CSCT = .7071 * SIN(BW2+TILTR)
      IF (RAD(M).LE.45.) GO TO 251
250  IREAM=0
      CONST=90./RAD(M)

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STATEMENT

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IF (BWD(M).EQ.360.) IBEAM=-1
GO TO 252
251 IBEAM=1
CONST=1.39157/SIN(BW2)
ANLL =ARSIN(PI/CONST)
CPAT1=10.**((13.2=SLDB(M)).*.05)
252 W = 983.573/FMHZ(M)
W4 = 0.25 * W
W LIM = 0.01 * W
FAC = PI2/W
PD = 2. * AHFT * S2
IF (INDEX .EQ. 1) GO TO 77
T23 = T2/ 3.
GAM = HAE/(SQRT (T23**2+HAE)+T23)
PSI = THET2 + GAM
S3 = SIN(PSI)
ZETA = PARAM * T2
D1=0.57735*SQRT(1.+2.*ZETA/SQRT(ZETA*ZETA+3))
PD1=SQRT(AH2+AEH*GAM*GAM)+2.*S3*S3
IF (ABS(PD-PD1).GE.W LIM) GO TO 79
79 IF (D1.LT.0.999) GO TO 79
780 D1 = 1.
INDEX = 1
79 PD = PD1
IF (PD.LT.W4.OR.THET2.LT.0.000873) GO TO 300
GO TO 301
301 IF (ICASH.NE.1) GO TO 300
302 CALL CASHOF
ICASH=0
300 CONTINUE
77 CALL SEARFF (FMHZ(M),PSI,IPAL,RHS,PHI)
PIZ=PI+Z+S3/W
PIZ2=PIZ*PIZ
RUF=EXP(-B.*PIZ2)
ANG = THET2 - TILTR
IF(IBEAM) 260,261,262
260 PAT=1.
GO TO 24
261 PAT=COS(CONST*ANG)
GO TO 24
262 IF (ICSC.NE.1) GO TO 61
80 IF (ANG.LE.AW2) GO TO 61
60 PAT = CSCT/S2
GO TO 24
61 IF (ANG.NE.0.) GO TO 23
22 PAT = 1.
GO TO 24
23 UU = CONST * SIN (ANG)
INT = UU/PI2
DIFF = UU - INT * PI2
IF (ABS(ANG).LE.ANLL) GO TO 161

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STATEMENT

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160 CPAT = CPAT1
    GO TO 162
161 CPAT = 1.
162 PAT = CPAT*SIN(DIFF)/UU
24  ANGR = THET2 + TILTR + 2. * GAM
    IF (IBEAM) 270,271,272
270 PATR=1.
    GO TO 27
271 PATR=CSS(CONST*ANGR)
    GO TO 27
272 IF (ANGR.NE.0.) GO TO 26
25  PATR = 1.
    GO TO 27
26  UUR = CONST * SIN(ANGR)
    INTR = UUR / PI2
    DIFFR = UUR - INTR * PI2
    IF (ABS(ANGR).LE.ANLL) GO TO 66
65  CPAT = CPAT1
    GO TO 67
66  CPAT = 1.
67  PATR = CPAT*SIN(DIFFR)/UUR
27  IF (ABS(PAT).GE.1.E-44) GO TO 29
28  IF (PAT.GE.0.) GO TO 281
280 D = -RHO*RUF*PATR*1.E45*D1
    GO TO 30
281 D=D1*RHO*RUF*PATR*1.E45
    GO TO 30
29  D = D1 * RHO * PATR/PAT * RUF
30  ALPHA = FAC * PD + PHI
    INT1 = ALPHA/PI2
    DIFF1 = ALPHA - INT1*PI2
    F = ABS(PAT)*SQRT(1.0 + D*D + 2.0*D*COS(DIFF1))
    RXN4(M)=(RFS(M)*F)**4
    PF4=PF4+SQRT(SGRT(RXN4(M)))/RNO
805 CONTINUE
    RNG=PF4
    RNG2=RNG*RNG
    RNG4=RNG2*RNG2
    FACMIN=10.
997 SUMEN=0.
    DO 998 MM=1,NRDS
        RRATIO=RXN4(MM)/RNG4
        PNO=FLOAT(NUM(MM))
        SUMEN=(PNO/PULS)*(RRATIO/(1.+GAMMA/RRATIO))+SUMEN
998 CONTINUE
    FACM2=FACMIN
    FACMIN=SUMEN*BETA
    FSUM=FACM2+FACMIN
    IF (RNG.EQ.0.) GO TO 993
    IF (ABS(FACMIN).LT.0.01) GO TO 993
    IF (FACMIN.GE.-1.) GO TO 902

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STATEMENT

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901 HONUM=4*INT(FACMIN)
    FACMIN=FACMIN-HONUM
902 CONTINUE
    RPREV=RNG
    RNG4=RNG4*(1.+FACMIN)
    RNG=SQRT(SQRT(RNG4))
    RDIFF=ABS (RPREV-RNG)
    IF (RDIFF.LT.0.1.AND.FSUM.LT.0.01) GO TO 993
    GO TO 997
993 CONTINUE
999 PFF(II)=RNG
910 CONTINUE
    THET2=THMINR-DEL1
    DO 806 II=1,IIMAX
        A=PFF(II)*EX
        THET2 = THET2 + DEL1
        N=N+1
        X = A * COS(THET2)
        Y = A * E * SIN(THET2)
    45 IF (X,LE,XMAX) GO TO 501
500 ISUMX=0
    GO TO 502
501 ISUMX=0
502 IF (Y,LE,YMAX) GO TO 504
503 ISUMY=0
    GO TO 505
504 ISUMY=0
505 IF (XP,LE,XMAX) GO TO 507
506 ISUMXP=0
    GO TO 508
507 ISUMXP=0
508 IF (YP,LE,YMAX) GO TO 510
509 ISUMYP=0
    GO TO 511
510 ISUMYP=0
511 ISUM=ISUMX+ISUMY+ISUMXP+ISUMYP+1
    GO TO (601,602,603,602,605,620,620,620,609,620,620,620,605,620),
    *ISUM
601 IF (N,NE,1) GO TO 3
    2 CALL PLOT (X,Y,3)
        X2=X
        Y2=Y
        XP=X
        YP=Y
        GOTO 806
    3 IF (N,NE,2) GO TO 440
44 YAXX
    YASY
    XP=X
    YP=Y
    X11=X

```

STATEMENT

```

Y11=Y
GOTO 806
440 CALL MINTAP (X,Y)
620 XP=X
    YP=Y
    IF (THET2.GE.THMAXR) GO TO 40
    GOTO 806
602 IF (N.EQ.1) GO TO 620
    CALL DASHON
    IDASH=0
    IF (IAXIS.EQ.1) CALL PLOT(XMAX,YMAX,2)
    CALL INTRST (0., YMAX,XMAX,YMAX,X,Y,YP,YP,X0,Y0)
621 CALL PLOT(X0,Y0,2)
    CALL DASHOF
    X2=X0
    Y2=Y0
    XA=X
    X11=X
    XP=X
    YA=Y
    Y11=Y
    YP=Y
    N=2
    GOTO 806
603 IF (N.EQ.1) GO TO 620
    CALL DASHON
    IDASH=0
    CALL INTRST (XMAX,0.,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
    GO TO 621
605 IF (N.EQ.1) GO TO 620
    CALL MINTAP (XP,YP)
    CALL PLAT(XP,YP,2)
    CALL INTRST (0.,YMAX,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
    IAXIS=2
    CALL PLOT(X0,Y0,2)
    GO TO 620
609 IF (N.EQ.1) GO TO 620
    CALL MINTAP (XP,YP)
    CALL PLOT(XP,YP,2)
    CALL INTRST (XMAX,0.,XMAX,YMAX,X,Y,XP,YP,X0,Y0)
    IAXIS=1
    CALL PLOT(X0,Y0,2)
    GO TO 620
40 IF (ISUM.NE.1) GO TO 651
650 CALL PLOT(X,Y,2)
    RETURN
651 IF (X.GT.XMAX.AND.XP.GT.XMAX) GO TO 652
    GO TO 653
652 CALL INTRST (XMAX,0.,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
    CALL DASHON
    IF (Y0.LE.YMAX) GO TO 655

```


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STATEMENT

```
654 CALL PLST(XMAX,YMAX,2)
    CALL INTRST (0.,YMAX,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
655 CALL PLST(X0,Y0,2)
    CALL DASHRF
    RETURN
656 IF (Y.GT.YMAX.AND.YP.GT.YMAX) GO TO 656
    GO TO 657
656 CALL DASHRF
    CALL INTRST (0.,YMAX,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
    IF (X0.LE.XMAX) GO TO 659
658 CALL INTRST (XMAX,0.,XMAX,YMAX,0.,0.,X,Y,X0,Y0)
660 CALL PLST(X0,Y0,2)
    CALL DASHRF
657 RETURN
659 IF(IAXIS.EQ.1) CALL PLST(XMAX,YMAX,2)
    GO TO 660
806 CONTINUE
    GOTO 809
807 PRINT 808
808 FORMAT(1H1,' END OF FILE HAS BEEN READ WHERE DATA CARD SHOULD BE')
809 END
```

STATEMENT

```

SUBROUTINE POSN(PDT,PFA,NPULS,KASE,SDR)
EXTERNAL PD
DIMENSION DB0(5),SLOPE(5),PDFAC(5)
COMMON /POS/ PFLAST,NLAST,KSLAST
DATA PFLAST/0./
DATA NLAST/0/
DATA KSLAST/-1/
DATA DB0/12.5,14.,14.,13.2,13.2/
DATA SLOPE/6.,7.,8.,7.,8./
DATA PDFAC/4.8,20.,20.,13.,13./
DATA DRMIN/-30./
DATA DRMAX/50./
DATA DB1/0./
DATA DB2/0./
DATA PDLAST/0./
IF (PDT.NE.PDLAST) GO TO 20
1 IF (PFA.NE.PFLAST) GO TO 20
2 IF (NPULS.NE.NLAST) GO TO 20
3 IF (KASE.EQ.KSLAST) RETURN
20 PDLAST=PDT
PFLAST=PFA
NLAST=NPULS
KSLAST=KASE
K=KASE + 1
PULS=NPULS
DR1=DB0(K)-SLOPE(K)+ALOG10(PULS)+(PDT-.5)*PDFAC(K)+(PFA-8.)*.4-1.
DR2=DR1+2.
CALL INVERS(DRMIN,DRMAX,DB1,DB2,4,15,NOI,SDR,PD1,PDT,PD)
END

```

STATEMENT

FUNCTION PD(SNOB)
COMMON/PDS/FA,I,KASE
NP=I
FAN=FA
KAS=KASE
CALL MARSAR (SNOB,NP,FAN,KAS,PD1)
PD=PD1
END

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STATEMENT

```

SUBROUTINE INVERS(XMIN,XMAX,XLO,XHI,NSIG,LIM,NOI,X,F1,FT,F)
TEST = 10.**(=-NSIG)
FD = FT
IF (FT.EQ. 0.) FD = 1.
NOI = 1
DELTA = XHI - XLO
X1=XLO
X2=XHI
F1=F(X1)
F2=F(X2)
SLOPE=(F2-F1)/(X2-X1)
IF (SLOPE.NE.0.) GO TO 21
10 FMAX=F(XMAX)
FMIN=F(XMIN)
SLOPE = (FMAX-FMIN)/(XMAX-XMIN)
21 IF ((F2-FT)*SLOPE.GE.0.) GO TO 23
22 X1=X2
F1=F2
X2=X2+DELTA
IF (X2.GT. XMAX) X2=XMAX
F2=F(X2)
GO TO 21
23 IF ((FT-F1)*SLOPE.GE.0.) GO TO 25
24 X2=X1
X1=X1-DELTA
IF (X1.LT. XMIN) X1=XMIN
F2=F1
F1=F(X1)
GO TO 23
25 XA=X1
XB=X2
F3=F2
IF (ABS (F2-FT).GE.ABS (F1-FT)) GO TO 6
7 F22=F2
F2=F1
F1=F22
X22=X2
X2=X1
X1=X22
GO TO 6
1 F1=F(X)
X1=X
TEST1 = ABS((F1-FT)/FD)
IF (TEST1.GT.TEST) GO TO 6
2 RETURN
6 IF(NOI.LT.LIM) GO TO 13
12 PRINT 40
PRINT 41, LIM
PRINT 42, XMIN, XMAX, XLO, XHI, NSIG, LIM, NOI, X, F1, FT
RETURN
13 IF (F1.NE.F2) GO TO 16

```

STATEMENT

```

15 IF (F1,FE,FB) GO TO 18
17 XR=X1
  X2=XR
  GO TO 19
18 XA=X1
  X2=XA
19 X=(XA+XB)*.5
  GO TO 1
20 Y=(X1-X2)*(F1-F2)/(F1-F2) + X2
  IF (X,LT,XA) X=XA
  IF (X,GT,XB) X=XB
  NSI = NSI + 1
  F2=F1
  X2=X1
  GO TO 1
40 FORMAT (// ' MESSAGE FROM SUBROUTINE INVERS == '//)
41 FORMAT (1 ' FUNCTION INVERSION NOT ACCOMPLISHED WITHIN SPECIFIED '
  * ',I3, ' ITERATIONS, '//)
42 FORMAT (// ' INVERS PARAMETERS WERE ',4(E10.3,2X),3(I3,2X),E10.3,
  * ' 2(2X,E10.3) '//)
  END

```


STATEMENT

```

SUBROUTINE MAPSWR (SNDR,N,FA,KASE,PN)
DOUBLE PRECISION ENPR,YBPR,GAMPR,PYB,H,Y0,E0,Y1,E1,STEP,YB
DOUBLE PRECISION DGAM, DEVAL, SUMLOG, SUML, FAN, FN
SNR = 10.**(SNDR*.1)
MODE=1
IF (MODE) 800, 800, 900
900 FAN=DLG10(DLOG(0.500)/DLOG(1.-(10.D0)**(-FA)))
GO TO 905
800 FAN = FA
905 IF(N) 99,99,2
2 IF(FA)99,99,3
3 IF(KASE) 99,4,4
4 IF(KASE=4) 5,5,99
5 ENPR = 0.
6 ENPR = FAN
EN = N
YBPR = 0.
IF (NPREV.EQ. N .AND. FAPREV.EQ. FA) GO TO 777
IF(N=12) 7,7,8
7 YBPR=EN*(1.+2.2*ENPR/EN**((2.00/3.D0)+0.015*ENPR))
GO TO 11
8 YBPR = EN*(1.+1.3*ENPR/EN**(.5+.011*ENPR))
11 ENPR = 10.**(ENPR)
GAMPR = DGAM(YBPR,N=1)
PYB = .5**((1./ENPR)
SUML = SUMLOG(N=1)
IF(GAMPR=PYB) 10,12,12
10 H = .01
GO TO 14
12 H = -.01
14 Y0 = YBPR
E0 = DEVAL(Y0,N=1,SUML)
16 Y1 = Y0+H
E1 = DEVAL(Y1,N=1,SUML)
STEP = GAMPR + H*(E0+E1)/2.
IF ((DSIGN(1.D0,STEP-PYB)=DSIGN(1.D0,H)).EQ.0.) GO TO 20
18 Y0 = Y1
E0 = E1
GAMPR = STEP
GO TO 16
20 IF(H) 22,24,24
22 YB = Y1 + H*(PYB-STEP)/(GAMPR-STEP)
GO TO 30
24 YB = Y0 + H*(PYB-GAMPR)/(STEP-GAMPR)
30 BIAS = YB
777 YB = BIAS
NPREV = N
FAPREV = FA
X = SNR
K = KASE+1
GO TO (100,200,300,400,500). K

```

STATEMENT

```

100 SUM = 0.
    P = EN**2
    IF (YB-P-EN) 150,102,102
102 KS = -(EN+1.)/2. + DSQRT(((EN+1.)/2.)**2+P*YB)
    KS = MAX0 (KS,0)
    GS = 1.-GAM(YB,KS+N-1,TN)
    TS = EVAL(P,KS)*GS
    G = GS
    K = KS
    TERM = TS
    TL = TN
110 TEMP = SUM+TERM
    IF (SUM-TEMP) 112,116,116
112 SUM = TEMP
    IF (K) 115,116,114
114 TERM = TERM*FLOAT (K)*(G+TL)/(P*G)
    G = G+TL
    K = K+1
    TL = TL*FLOAT (K+N)/YB
    GO TO 110
116 TL = TN*YB/FLOAT (KS+N)
    K = KS+1
    G = GS+TL
    TERM = TS+P*G/(GS*FLOAT (K))
120 TEMP = SUM+TERM
    IF (SUM-TEMP) 122,190,190
122 SUM = TEMP
    TL = TL*YB/FLOAT (K+N)
    K = K+1
    TERM = TERM*P*(G+TL)/(G*FLOAT (K))
    G = G+TL
    GO TO 120
150 KS = -1. - EN/2. + DSQRT(EN**2/4.+P*YB)
    KS = MAX0 (KS,0)
    GS = GAM(YB,KS+N-1,TN)
    IF (GS) 174,174,155
155 TS = EVAL(P,KS)*GS
    G = GS
    TERM = TS
    K = KS
    TL = TN
160 TEMP = SUM+TERM
    IF (SUM-TEMP) 162,166,166
162 SUM = TEMP
    IF (K) 165,166,164
164 TERM = TERM*FLOAT (K)*(G+TL)/(P*G)
    G = G+TL
    TL = TL*FLOAT (K+N-1)/YB
    K = K+1
    GO TO 160
166 TL = TN*YB/FLOAT (KS+N)

```

STATEMENT

```

K = K+1
G = GS-TL
TERM = TS*P*G/(GS*FLOAT (K))
170 TEMP = SUM + TERM
IF(SUM=TEMP) 172,174,174
172 SUM = TEMP
TL = TL*YB/LOAT (K+N)
TERM = TERM*P*(G-TL)/(G*LOAT (K+1))
G = G-TL
K = K+1
GO TO 170
174 SUM = 1.-SUM
190 PN = SUM
GO TO 90
200 IF(N=1) 210,210,220
210 PN = DEXP(-YB/(1.+X))
GO TO 90
220 TEMP = 1. + 1./(EN*X)
PN = 1. - GAM(YB,N=2,DUM) + DEXP((EN-1.)*ALOG(TEMP)-YB/(1.+EN*X))
*      *GAM(YB/TEMP,N=2,DUM)
GO TO 90
300 IF(N=1) 310,310,320
310 PN = DEXP(-YB/(1.+X))
GO TO 90
320 PN = 1. - GAM(YB/(1.+X),N=1,DUM)
GO TO 90
400 IF(N=2) 410,420,430
410 PN = (1.+2.*X*YB/(X+2.))*DEXP(-2.*YB/(2.+X))
GO TO 90
420 PN = (1.+YB/(1.+X))*DEXP(-YB/(1.+X))
GO TO 90
430 C = 2./(2.+EN*X)
D = 1.-C
IF(YB*D=EN) 440,450,450
440 SUM = 0.
TERM = 1.
J = N
442 TEMP = SUM+TERM
IF(SUM=TEMP) 444,446,446
444 SUM = TEMP
TERM = TERM*YB*D/LOAT (J)
J = J+1
GO TO 442
446 PN = 1. - GAM(YB,N=2,DUM) + C*YB*EVAL(YB,N=2)
*      + D*EVAL(YB,N=1)*(1.+C*YB-(EN=2.)*C/D)*SUM
GO TO 90
450 PN = 1. - GAM(YB,N=3,DUM) + YB*EVAL(YB,N=3)*C/D
*      + DEXP(-C*YB-(EN=2.)*ALOG(D))*(1.+C*YB-(EN=2.)*C/D)
*      *GAM(YB*D,N=3,DUM)
GO TO 90
500 SUM = 0.

```

STATEMENT

```

C = 2./(2.+X)
D = 1.-C
G = C/D
P = C*YB
KS = (3.+EN+(YB*D))/2.-DSGRT((EN-1.+(YB*D))**2/4.+(YB*D)*(EN+1.))
KS = MIN0 (KS,N)
KS = MAX0 (KS,0)
K = KS
J = N-KS
FKS = KS
K = MIN0 (KS,N)
IF (YB-FN*(1.+D)) 550,501,501
501 GS = 1. - GAM(P,2*N-1-KS,TN)
IF (GS) 526,526,502
502 TS = DEXP(FKS*ALOG(C)+(EN-FKS)*ALOG(D)+SUMLOG(N)-SUMLOG(KS)
* -SUMLOG(J)+ALOG(GS))
G = GS
TERM = TS
TL = TN
510 TEMP = SUM+TERM
IF (SUM=TEMP) 512,516,516
512 SUM = TEMP
IF (K) 516,516,514
514 TL = TL+P/FL0AT (2*N-K)
TERM = TERM+FL0AT (K)*(G+TL)/(G*FL0AT (N-K+1)*G)
G = G+TL
K = K+1
GO TO 510
516 IF (KS=N) 518,526,526
518 TERM = TS+G*FL0AT (N-KS)*(GS-TN)/(FL0AT (KS+1)+GS)
G = GS-TN
TL = TN+FL0AT (2*N-1-KS)/P
K = KS+1
520 TEMP = SUM+TERM
IF (SUM=TEMP) 522,526,526
522 SUM = TEMP
IF (K=N) 524,526,526
524 TERM = TERM+G*FL0AT (N-K)*(G+TL)/(FL0AT (K+1)+G)
G = G+TL
TL = TL+FL0AT (2*N-1-K)/P
K = K+1
GO TO 520
526 PN = SUM
GO TO 90
550 GS = GAM(P,2*N-1-KS,TN)
IF (GS) 576,576,552
552 TS = DEXP(FKS*ALOG(C)+(EN-FKS)*ALOG(D)+SUMLOG(N)-SUMLOG(KS)
* -SUMLOG(J)+ALOG(GS))
G = GS
TERM = TS
TL = TN

```


STATEMENT

```

560 TEMP = SUM+TERM
    IF (SUM=TEMP) 562,566,566
562 SUM = TEMP
    IF (K) 566,566,564
564 TL = TL+P/FL0AT (2+N-K)
    TERM = TERM+FL0AT (K)*(G+TL)/(G+FL0AT (N-K+1)*G)
    G = G+TL
    K = K+1
    GO TO 560
566 IF (KS=N) 568,576,576
568 TERM = TS+Q*FL0AT (N-KS)*(GS+TN)/(FL0AT (KS+1)*GS)
    G = GS+TN
    TL = TN*FL0AT (2+N-1-KS)/P
    K = KS+1
570 TEMP = SUM+TERM
    IF (SUM=TEMP) 572,576,576
572 SUM = TEMP
    IF (K=N) 574,576,576
574 TERM = TERM+Q*FL0AT (N-K)*(G+TL)/(FL0AT (K+1)*G)
    G = G+TL
    TL = TL*FL0AT (2+N-1-K)/P
    K = K+1
    GO TO 570
576 PN = 1.-SUM
    GO TO 90
90 IF (PN) 91,94,92
91 PN = 0.
    GO TO 94
92 IF (PN=1.) 94,94,93
93 PN = 1.
94 RETURN
99 WRITE (61,9) N,FA ,SNR,KASE
9 FORMAT (1H0 /50H UNREASONABLE CALL SEQUENCE TO MARCUM, ZERO RESULT
*      7HS GIVEN //4H N = 18,5X,5HFA = E16.8,5X,5HSNR =
*      E16.8,5X,6HKASE = 18)
    PN = 0.
    BIAS = 0.
    RETURN
END

```

STATEMENT

```

FUNCTION DGAM(B,N)
DOUBLE PRECISION SUM, TERM,TEMP,FJ,DGAM, DEVAL, R, SUML,SUMLOG
SUM = 0.
K = R
IF(K=N) 100,200,200
100 J = N+1
SUML = SUMLOG(J)
TERM = DEVAL(B,J,SUML)
10 TEMP = SUM+TERM
IF(SUM-TEMP) 15,20,20
15 SUM = TEMP
J = J+1
FJ = J
TERM = TERM*B/FJ
GO TO 10
20 DGAM = SUM
RETURN
200 J = N
SUML = SUMLOG(J)
TERM = DEVAL(B,J,SUML)
30 TEMP = SUM+TERM
IF(SUM-TEMP) 35,40,40
35 SUM = TEMP
IF(J-1) 40,36,36
36 FJ = J
TERM = TERM*B/FJ
J = J-1
GO TO 30
40 DGAM = 1.-SUM
RETURN
END

```

STATEMENT

```
FUNCTION DEVAL (Y,N,SUML)
DOUBLE PRECISION XPN,EN,DEVAL, Y,SUML
XPN = -Y
IF(N) 20,20,10
10 EN = N
XPN = XPN+EN+DLOG(Y)-SUML
20 DEVAL = DEXP(XPN)
RETURN
END
```

STATEMENT

```

FUNCTION GAM(R,N,TN)
SUM = 0.
K = 8
IF(K=N) 100,200,200
100 J = N+1
    TERM = EVAL(R,J)
    TN = TERM*FLOAT(J)/R
10 TEMP = SUM+TERM
    IF(SUM+TEMP) 15,20,20
15 SUM = TEMP
    J = J+1
    FJ = J
    TERM = TERM*R/FJ
    GO TO 10
20 GAM = SUM
    RETURN
200 J = N
    TERM = EVAL(R,J)
    TN = TERM
30 TEMP = SUM+TERM
    IF(SUM+TEMP) 35,40,40
35 SUM = TEMP
    IF(J=1) 40,30,30
30 FJ = J
    TERM = TERM*R/FJ
    J = J+1
    GO TO 30
40 GAM = 1.-SUM
    RETURN
END

```


STATEMENT

```
FUNCTION EVAL(Y,N)  
  XPRN = -Y  
  IF(N) 20,20,10  
10 EN = N  
  XPRN = XPRN+EN*ALOG(Y)-SUMLOG(N)  
20 EVAL = EXP (XPRN)  
  RETURN  
END
```

STATEMENT

```

FUNCTION SUMLOG(N)
DOUBLE PRECISION A, B, SUMLOG
DIMENSION A(1000)
DATA DUMA / 0./
DATA DUMB / 0./
DATA NLAST/1/
NMAX=1000
IF(DUMA=DUMB) 20,10,20
10 DUMA = 1.
   DUMB = 0.
   NLAST = 1
   A(1) = 0.
20 NN = IABS (N)
   IF(NN=1) 30,30,40
30 SUMLOG = 0.
   RETURN
40 IF(NN=NLAST) 50,50,60
50 SUMLOG = A(NN)
   RETURN
60 K = NLAST+1
   IF(NN=NMAX) 70,70,80
70 DO 72 I=K,NN
72 A(I) = A(I-1) + DLOG(DFLOAT(I))
   NLAST = NN
   GO TO 50
80 IF(NLAST=NMAX) 82,90,90
82 DO 84 I=K,NMAX
84 A(I) = A(I-1) + DLOG(DFLOAT(I))
   NLAST = NMAX
90 B = A(NMAX)
   K = NMAX+1
   DO 92 I=K,NN
92 B = B + DLOG(DFLOAT(I))
   SUMLOG = B
   RETURN
END

```

STATEMENT

```

SUBROUTINE RHACHT(XMAX,YMAX,RMAX,HMAX,ANTHGT)
EXTERNAL F1
DIMENSION SN(181), RIG1(181), TNI(181), JA(6)
DIMENSION XZ(180),YZ(180)
DIMENSION IRFAC(5), IHFAC(8)
COMMON /A/ REF, GRAD, RAD, CONST, U(182), V
COMMON /XTYPE/ X22,Y22,X11,Y11,XAA,YAA,ERROR
DIMENSION IANG(9),AANG(9)
COMMON /B/ XX(181), YY(181), CT1(181), SN1(181), DEL
DATA ERROR / .001/
DATA REF/.000313/
DATA GRAD/.0000438422/
DATA IANG/1,26,31,51,71,121,151,172,181/
DATA AANG/0.,.5,1.,3.,5.,10.,30.,60.,90./
DATA IHFAC/50,100,500,1000,5000,10000,50000,100000/
DATA IRFAC/5,10,50,100,500/
DATA JA/31,51,71,121,151,172/
CALL PENCHG(10)
DEL=XMAX*.01
IF (YMAX.LT.XMAX) DEL=YMAX*.01
BA = 6.076.1155*RMAX*YMAX/(HMAX*XMAX)
BA2 = BA*BA
PREC = .00001
CONST = .3048/1852.0
RAD=20698950.13*ANTHGT
AB = 1.0 + REF
AB2 = AB*AB
CD = 2.0 + REF + REF*REF
ELEV = -.02
II=0
DO 29 JI=1,6
GO TO (490,491,492,493,494,495), JI
490 ADEL = .02
MM=26
GO TO 51
491 ADEL = .1
MM=95
GO TO 51
492 ADEL=.5
MM=20
GO TO 51
493 ADEL = 1.0
MM=25
GO TO 51
494 ADEL=2.5
MM=12
GO TO 51
495 ADEL=5.0
MM=3
51 DO 29 IK = 1,MM
II=II+1

```

STATEMENT

```

ELEV=ELEV+ADEL
RDN = ELEV/57.29577957
SN(II) = SIN(RDN)
S = SN(II)**2
U(II) = AB2*S-CD
IF (II,GE,181) GO TO 361
360 TN = TAN (RDN)
RDN1 = ATAN (BA*TN)
TN1(II) = TAN (RDN1)
CT1(II) = COS(RDN1)
SN1(II) = SIN(RDN1)
GO TO 29
361 CT1(II) = 0.0
SN1(II) = 1.0
29 CONTINUE
B=BA*YMAX
DO 290 IX= 1,180
BAT=SQRT(BA2+(TN1(IX))**2)
YZ(IX)=XMAX*BA/BAT
290 YZ(IX)=B*TN1(IX)/BAT
H1 = 0.0
IJM = 100
JMAX = INT (ALOG10(HMAX) + .477122)
HINT=10.**(JMAX-1)
IJG = (HMAX/(10.**(JMAX-1)) + .001)
HMX=IJG*10.**(JMAX-1)
DO 30 J = 1, JMAX
IF (J,EG, JMAX) IJM = IJG
IF (J,NE,1) GO TO 3
2 IJ = 10
GO TO 4
3 IJ = 20
4 DO 30 I = IJ,IJM,10
H2 = I * 10 ** (J - 1)
IF(H2,EQ,HMX) CALL PENCHG(11)
DO 304 K = 1, 181
N=182-K
IF (H2,EG, 10 .) RNG1(N) = 0.0
IF (H2,EQ,10..AND,N,EQ,1) GO TO 6
GO TO 7
6 GAM = REF*GHAD/AB
RI = 1.0/RAD
GG = 2.0*(RI - GAM)
RNG2 = (CONST*AB/GG)+2.0*SQRT(GG*H2)
GO TO 8
7 CALL SINCON (H1,H2,PREC ,15,RINC,N01,R,F1)
RNG2 = RNG1(N) + RINC
8 RNG1(N) = RNG2
IF (H2,LT, HINT) GO TO 304
A = RNG2*YMAX/RHAX
B = BA+A

```


STATEMENT

```

IF (N,NE,181) GO TO 47
46 CALL PLST (0.,8,3)
XX(181) = 0.
YY(181) = 8
X=0.
Y=8
X22=0.
Y22=8
GO TO 304
47 XLAST = X
YLAST = Y
X=A+XZ(N)/XMAX
Y=A+YZ(N)/YMAX
48 IF (H2,NE,-HMAX) GO TO 68
87 XX(N)=X
YY(N)=Y
68 IF (K,NE,2) GO TO 781
780 X11=X
Y11=Y
XAA=X
YAA = Y
GO TO 304
781 IF (X,LE,(XZ(N)+.0001)) GO TO 783
782 CALL INTST (XLAST,YLAST,X,Y,XZ(N),YZ(N),XZ(N+1),YZ(N+1),X0,Y0)
CALL MINTAP (X0,Y0)
CALL PLST (X0,Y0,2)
IF (H2,EG,HMAX) GO TO 785
GO TO 305
783 IF (K,NE,181) GO TO 789
787 CALL MINTAP (X,Y)
CALL PLST(X,Y,2)
XCOR = X
YCOR = Y
GO TO 304
788 CALL MINTAP (X,Y)
304 CONTINUE
305 H1 = H2
30 CONTINUE
GO TO 789
785 CALL PLST(XZ(1),0.,3)
DO 786 NK=1,N
XX(NK)=XZ(NK)
YY(NK)=YZ(NK)
786 CALL PLST(XX(NK),YY(NK),2)
CALL PLST(X0,Y0,2)
XCOR = X0
YCOR = Y0
789 X=0.
Y = YMAX
CALL PLST(X,Y,3)
Y = 0.0

```

STATEMENT

```

CALL PLST(X,Y,2)
X=XMAX
CALL PLST(X,Y,2)
CALL PENCHG(10)
KAM=XMAX=1.
INTR=10
IF(RMAX,LT. 100.) INTR=5
IF(RMAX,GT. 300.) INTR=25
DO 31 KA=INTR,KAM,INTR
RG = KA
A = RG*XMAX/RMAX
B = BA+A
DO 3A KC = 1, 181
KR=KC
IF (KC,NE.181) GO TO 92
91 CALL MINTAP (0.,B)
CALL PLST(0.,B,2)
GO TO 31
92 X=A*XZ(KC)/XMAX
IF (X,GT,XX(1)) GO TO 31
Y=A*YZ(KC)/XMAX
IF (Y,LE.(YY(KC)+.0001)) GO TO 72
73 IF (KR,NE.N+1) GO TO 731
730 X1=XCOR
Y1=YCOR
GO TO 732
731 X1=XX(KR-1)
Y1 = YY(KR-1)
732 X2=XX(KR)
Y2 = YY(KR)
XR=X
YB = Y
CALL INTRST (X1,Y1,X2,Y2,XA,YA,XB,YB,X0,Y0)
CALL PLST(X0,Y0,2)
GO TO 31
72 XA = X
YA = Y
IF (KC,NE.1) GO TO 86
85 CALL PLST(X,Y,3)
X22=X
Y22=Y
GO TO 3A
86 IF (KC,NE.2) GO TO 861
860 X11=X
Y11=Y
XAA=X
YAA=Y
GO TO 3B
861 CALL MINTAP (X,Y)
3A CONTINUE
31 CONTINUE

```

STATEMENT

```

700 CALL ATICK(1,26,5,4,5)
    CALL ATICK(27,71,1,5,10)
    CALL ATICK(73,141,2,0,5)
    CALL ATICK(142,151,1,0,5)
    CALL ATICK(156,166,5,0,2)
    CALL ATICK(168,178,2,1,2)
    CALL ATICK(179,181,1,1,2)
    DO 34 KF = 1, 6
    NF = JA(KF)
    X = 0.0
    Y = 0.0
    CALL PLOT(X,Y,3)
    X = XX(NF)
    Y = YY(NF)
    CALL PLOT(X,Y,2)
34 CONTINUE
    KT = 9
    DO 364 KY = 1, 800
    KT = KT + 1
    IF (KT.NE.10) GO TO 369
368 FAC = 2.0
    KT = 0
    GO TO 370
369 FAC = 1.0
370 R2 = KY = 1
    X = R2*XMAX/RMAX
    IF (X.GT.(XMAX + .0001)) GO TO 365
    Y = 0.0
    CALL PLOT(X,Y,3)
    Y = - FAC * DEL
    CALL PLOT(X,Y,2)
364 CONTINUE
365 KS = 9
    KJM = HMAX / HINT + 1.001
    DO 37 KJ = 1, KJM
    KS = KS + 1
    IF (KS.NE.10) GO TO 376
375 FAC = 2.0
    KS = 0
    GO TO 377
376 FAC = 1.0
377 H = HINT * (KJ - 1)
    Y = H*YMAX/HMAX
    X = 0.0
    CALL PLOT(X,Y,3)
    X = - FAC * DEL
    CALL PLOT(X,Y,2)
37 CONTINUE
    CALL PENCHG(11)
    IF (XMAX=YMAX) 460,460,461
460 SFAC=XMAX +.125

```

STATEMENT

```

      GO TO 402
401 SPAC=YMAX*.125
402 H=.175*SPAC
      DO 100 I= 1, 5
      NR = RMAX / IRFAC (IR)
      IF (NR.GT.10) GO TO 100
101 IRUNIT = IRFAC (IR)
      GO TO 102
100 CONTINUE
      IRUNIT=IRFAC(5)
102 DO 110 IH = 1, 8
      NH = HMAX / IHFAC (IH)
      IF (NH.GT.10) GO TO 110
103 IHUNIT = IHFAC (IH)
      GO TO 128
110 CONTINUE
      IHUNIT=IHFAC(8)
128 X=-.05*SPAC
      Y=-.5*SPAC
      CALL INUMBR (X,Y,H,0,0.0)
      N = IRUNIT
120 IDGITS=ALOG10(FLCAT(N))+1.000001
      CALL SENTER (H,IDGITS,IDGITS,BIAS)
      X = (N/RMAX) * XMAX = BIAS
      IF (X + BIAS .GT. XMAX) GO TO 801
      CALL INUMBR (X,Y,H,N,0.0)
      N = N + IRUNIT
      GO TO 120
801 Y=-1.0*SPAC
      CALL SENTER (H, 21,21,BIAS)
      X = 0.5 * XMAX = BIAS
      CALL LETTER (X,Y,H,21H RANGE, NAUTICAL MILES,0.0,21)
      X=-.5*SPAC
      Y=-.0875*SPAC
      CALL INUMBR (X,Y,H,0,0.0)
      N = IHUNIT
121 IHGITS=ALOG10(FLCAT(N))+3.000001
      X=-0.15*IHGITS*SPAC
      Y=(N/HMAX)*YMAX=.0875*SPAC
      IF (Y .GT. YMAX) GO TO 803
      CALL INUMBR (X,Y,H,N,0.0)
      N = N + IHUNIT
      GO TO 121
803 X = -1.40*SPAC
      CALL SENTER(H,33,33,BIAS)
      Y = 0.5 * YMAX = 9145
      CALL LETTER (X,Y,H,33H TARGET HEIGHT ABOVE ANTENNA, FEET,90.,33)
      X1=X-3.*H
      CALL SENTER(H,26,26,BIAS)
      CALL LETTER (X1,Y,H,26H (ANTENNA HEIGHT= FEET),90.,26)
      Y2=Y+10.5714*H

```


STATEMENT

```

CALL NUMBER (X1,Y2,H,ANTHGT,90.,-1)
XPR= 2.*XMAX
YPR=2.0*H
DO 804 IL = 1, 9
  IND = IANG(IL)
  AAN=AAAG(IL)
  CX=.1
  IF (IL.GE.6)CX=.125
  X=XX(IND) + .4*CT1(IND)*SFAC = CX*SFAC
  Y=YY(IND) + .4*SN1(IND)*SFAC = .0875*SFAC
  IF (IL.EG. 9) X = X - H
  IF (IL.EQ.9 .OR. (Y-YPR).GT.(1.5*H)) GO TO 880
  IF ((XPR-X).LT.(4.0*H) .OR. X.LT.2.*H) GO TO 804
880 XPR=X
  YPR=Y
  IF (IL.GE.6) GO TO 888
887 CALL NUMBER (X,Y,H,AAN,0.0,1)
  X = X + .15 * SFAC
  GO TO 889
888 CALL NUMBER (X,Y,H,AAN,0.0,-1)
889 CONTINUE
  CALL DEGREE (X + .35*SFAC, Y + .175 * SFAC,.08*SFAC)
804 CONTINUE
END

```

STATEMENT

```
FUNCTION F1(X)
COMMON /A/ REF, GRAD, RAD, CONST, U(162), N
BB=REF*EXP(-GRAD*X)
CC=X/RAD
V=2.0*BB+BB*BB
A=2.0*CC+CC*CC
FX = SQRT (U(N) + V + A + V*A)
F1 = CONST * (1.0 + V)*(1.0 + CC)/FX
END
```

STATEMENT

```

SUBROUTINE SIMCON(X1,XEND,TEST,LIM,AREA,NOI,P,F)
NOI=0
CDD=0.0
INT=1
V=1.0
EVEN=0.0
AREA1=0.0
19 ENDS=F(X1)+F(XEND)
2 H=(XEND-X1)/V
CDD=EVEN+CDD
X=X1+H/2.
EVEN=0.0
DO 3 I=1,INT
21 EVEN=EVEN+F(X)
X=X+H
3 CONTINUE
31 AREA=(ENDS+4.0*EVEN+2.0*CDD)*H/6.0
NOI=NOI+1
34 R=ABS((AREA1-AREA)/AREA)
IF(NOI=LIM)341,35,35
341 IF(R=TEST)35,35,4
35 RETURN
4 AREA1=AREA
46 INT=2*INT
V=2.0*V
GO TO 2
END

```

STATEMENT

```

SUBROUTINE ATICK (IA,JA,KA,MR,MC)
COMMON /R/ XX(161), YY(161), CT1(161), SN1(161), DEL
MA = MR
DO 1 K = IA,JA,KA
MA = MA + 1
IF (MA,ME,MC) GO TO 3
2 FAC = 2.0
MA = 0
GO TO 4
3 FAC = 1.0
4 X = XX(K)
Y = YY(K)
CALL PLOT(X,Y,3)
X = X + DEL*FAC*CT1(K)
Y = Y + DEL*FAC*SN1(K)
CALL PLOT(X,Y,2)
1 CONTINUE
END
```

STATEMENT

```
SUBROUTINE SENTER (M,N,I,RIAS)
CONST = .2857143 * M
WIDTHF = (3*I-1) * CONST
WIDTHN = (3*N-1) * CONST
RIAS = WIDTHF = 0.5 * WIDTHN
RETURN
END
```


STATEMENT

```

SUBROUTINE MINTAP (X,Y)
COMMON /MTPE/ X2, Y2, X1, Y1, XA, YA, ERRPR
COMMON /XA/ M,N
DATA N/0/
DATA N/0/
DX(U1,V1,U2,V2) = SQRT((U2-U1)**2 + (V2-V1)**2)
D1 = DX(X1,Y1,X2,Y2)
IF (D1 .EQ. 0.) GO TO 11
U2 = DX(X,Y,X1,Y1)
IF (D2 .EQ. 0.) GO TO 2
D3 = DX(X,Y,X2,Y2)
D11 = DX(XA,YA,X2,Y2)
IF (D3 .LT. D11) GO TO 1
COSN = (D3*D3-D2*D2-D1*D1)/(2.*D1*D2)
IF (COSN .GT. 1. .OR. COSN .LT. -1.) COSN = 1.
SINE = SQRT(1. - COSN*COSN)
DEVN = D2*SINE
IF (DEVN .LE. ERRPR) GO TO 2
1 CALL PLST (XA,YA,2)
M = M+1
X2 = XA
Y2 = YA
11 X1 = X
Y1 = Y
2 XA = X
YA = Y
N = N+1
END

```

STATEMENT

```

SUBROUTINE SEAREP (FMHZ, PSI, IPOL, RHO, PHI)
      COMPLEX EPSC, GAM, SQTERM, TERM
      DATA FLAST / 0./
      SINPSI = SIN (PSI)
      CSPSI = COS(PSI)**2
      IF (FMHZ.EQ. FLAST) GO TO 200
      FLAST = FMHZ
      * = 299.793 / FMHZ
      IF (FMHZ.GT. 1500.) GO TO 151
150 SIG = 4.3
      EPS1 = 80.
      GO TO 155
151 SIG = 4.3 + (FMHZ - 1500.) * .00148
      IF (FMHZ.GT. 3000.) GO TO 154
153 EPS1 = 80. - (FMHZ - 1500.) * .00733
      GO TO 155
154 EPS1 = 89. - (FMHZ - 3000.) * .002429
      SIG = 6.52 + (FMHZ - 3000.) * .001314
155 EPSC = CMPLX (EPS1,-60.*SIG)
200 SQTERM= CSQRT(EPSC-CSPSI)
      IF (IPOL.NE. 1 ) GO TO 161
160 TERM =      EPSC * SINPSI
      GAM = (TERM-SQTERM)/(TERM+SQTERM)
      GO TO 180
161 GAM = (SINPSI * SQTERM) / (SINPSI + SQTERM)
180 RHO = CABS (GAM)
      PHI =-ATAN2 (AIMAG(GAM), REAL (GAM))
      RETURN
      END

```

STATEMENT

```
SUBROUTINE DEGREE(X,Y,H)
  DIMENSION DELX(8), DELY(8)
  DATA DELX/-0.7071,-1.0,-0.7071,0.0,0.7071,1.0,0.7071,0.0/
  DATA DELY/0.7071,0.0,-0.7071,-1.0,-0.7071,0.0,0.7071,1.0/
  D = H*.414214
  X = X + .5*H
  Y = Y + .5*D
  CALL PLOT (X,Y,3)
  DO 1 II = 1, 8
    X = X + DELX(II)*D
    Y = Y + DELY(II)*D
  1 CALL PLOT(X,Y,2)
  END
```

STATEMENT

```

SUBROUTINE INTERST (X1,Y1,X2,Y2,XA,YA,XB,YB,X0,Y0)
  IF (ABS(X2-X1).GE.10,E=76) GO TO 2
1  IF (ABS(X2-XA).LT.10,E=76) GO TO 99
  X0 = X1
  S = (Y2-YA)/(XB-XA)
  Y0 = S*(X0-XA) + YA
  RETURN
2  IF (ABS(XB-XA).GE.10,E=76) GO TO 4
3  IF (ABS(X2-X1).LT.10,E=76) GO TO 99
  X0 = XA
  S = (Y2-Y1)/(X2-X1)
  Y0 = S*(X0-X1) + Y1
  RETURN
4  S1 = (YB-YA)/(XB-XA)
  S2 = (Y2-Y1)/(X2-X1)
  IF (S1.EQ. 0.) GO TO 5
  IF (ABS(S2-S1).LT.10,E=76) GO TO 99
  RTO = S2/S1
  Y0 = (Y2+S2*(XA-X2)-YA*RTO)/(1.-RTO)
  X0 = (Y0-YA)/S1 + XA
  RETURN
5  IF (S2.EQ. 0.) GO TO 99
  X0 = (YA-Y2)/S2 + X2
  Y0 = YA
  RETURN
99 PRINT 100, X1, Y1
  PRINT 101, X2,Y2,XA,YA,XB,YB
  X0 = 0.
  Y0 = 0.
100 FORMAT (IX,64HCALL TO INTERSECT ABORTED. LINES PARALLEL, NO INTERSE
  *CTION. X1 = ,E10.2,6H Y1 = ,E10.2)
101 FORMAT(IX,64H X2 = ,E10.2,6H Y2 = ,E10.2,
  * 6H XA = ,E10.2,6H YA = ,E10.2,6H XB = ,E10.2,6H YB = ,E10.2 //)
  END

```

STATEMENT

```
SUBROUTINE ARRA (X1,Y1,X2,Y2,TIPL)
COMMON/AG/ANG
DATA ANG / .35/
YA = Y2 - Y1
XA = X2 - X1
A = ATAN2(YA,XA)
A3 = A + ANG
A4 = A - ANG
X3 = X2 - TIPL * COS(A3)
Y3 = Y2 - TIPL * SIN(A3)
X4 = X2 - TIPL * COS(A4)
Y4 = Y2 - TIPL * SIN(A4)
CALL PLOT (X1, Y1, 3)
CALL PLOT (X2, Y2, 2)
CALL PLOT (X3, Y3, 2)
CALL PLOT (X4, Y4, 3)
CALL PLOT (X2, Y2, 2)
END
```

STATEMENT

```
SUBROUTINE REZERO
ENTRY PENCHG
ENTRY DASHON
ENTRY DASHOF
END
```


APPENDIX B: Input Data Card Formats for LOBMUF (For ASC - Jan 1977)

Program LOBMUF will plot the envelope of N radars using the pattern calculations contained in the original program described in NRL Report 7098 by L. Blake. Incoherent integration is assumed. An antenna height must be specified in subroutine RHACHT. The parameter name for this antenna height is ANTHITE and is used to draw the range-height grid. The actual antenna heights for the individual radars are input separately and used for the multipath calculations. ANTHITE is not very important except for the labeling of the height axis of the grid.

Input Card Sequence

Col.

1. ANTHITE in F10.0 field
2. Label Card
3. Grid Parameters in F10.0 fields:
 - a. XMAX 1-10
 - b. YMAX 11-20
 - c. RMAX 21-30
 - d. HMAX 31-40
 - e. THMIN 41-50
 - f. THMAX 51-60
 - g. WHFT 61-70
 - h. RDR 71-80

XMAX = maximum X-dimension of chart in inches

YMAX = maximum Y-dimension of chart in inches

RMAX = maximum range of chart in nautical miles

HMAX = maximum height on chart in feet

THMIN = minimum elevation angle for the plot

THMAX = maximum elevation angle for the plot

WHFT = sea wave height in feet

RDR = number of radars for which an envelope is to be plotted.

4. Common Parameters in F10.0 fields:
 - a. PDT 1-10
 - b. PFA 11-20
 - c. PULS (total number of pulses) 21-30
 - d. CASE 31-40
 - e. AHFT 41-50
 - f. TILT 51-60
 - g. POL 61-70
 - h. CSC 71-80

PDT = probability of detection

PFA = false alarm exponent, i.e., the positive value of the exponent (power of ten); for 10^{-6} , enter the number 6.0, etc.

PULS = total number of pulses

CASE = Swerling case number
AHFT = antenna height in feet
TILT = tilt angle of the antenna beam maximum with
respect to the horizon in degrees.

For reference, POL is polarization as follows:

POL = 1. vertical
POL = 2. horizontal

CSC is for pencil or cosecant squared antenna pattern:

CSC = 0. pencil beam
CSC = 1. cosecant squared beam

5. Radar Parameters in F10.0 fields:

a. RFS	1-10
b. FMHZ	11-20
c. BWD	21-30
d. SLDB	31-40
e. PULNUM (number pulses at FMHZ)	41-50
f. FREF	51-60

Repeat card 5 for N repetitions.

RFS = calculated or assumed free-space range of the
radar on the specified target
FMHZ = radar frequency in megahertz
BWD = antenna half-power beamwidth in degrees
SLDB = first elevation sidelobe level relative to the
main lobe
PULNUM = number of pulses at each specified frequency
FREF = frequency used to calculate RFS if RFS was
calculated for the total number of pulses (PULS)
FREF = 0, if RFS was calculated at each frequency using
PULNUM.

After cards 1-5, the sequence can be repeated as many times as desired,
starting with card 2.

A note of caution is that the elevation plot angle increment is
determined by

$$\frac{THMAX - THMIN}{2000}$$

The value has proven adequate for S-band radars where 10° and 0° were the
values for THMAX and THMIN. It is recommended that an envelope for a
single radar (RDR = 1) be run when there is doubt that this angle increment
is small enough.